

## Multiple Springs

### Problems:

Determine the effective spring constant for each of the following (all spring constants are given in N/m.):

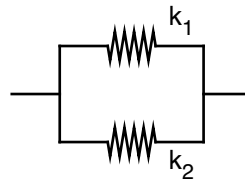
1.  $k_1 = 50$  &  $k_2 = 75$



$$\frac{1}{k_e} = \frac{1}{50} + \frac{1}{75} = \frac{5}{150}$$

$$\frac{1}{k_e} = \frac{1}{30} \rightarrow \boxed{k_e = 30 \text{ N/m}}$$

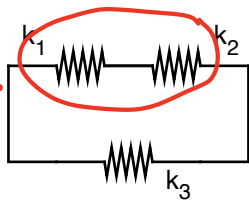
2.  $k_1 = 50$  &  $k_2 = 75$



$$k_e = 50 + 75$$

$$\boxed{= 125 \text{ N/m}}$$

3.  $k_1 = 10$  &  $k_2 = 30$  &  $k_3 = 20$



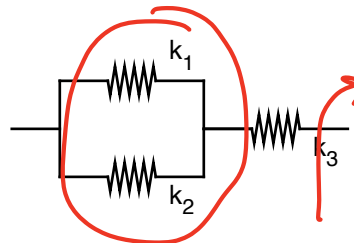
$$\frac{1}{k_e} = \frac{1}{10} + \frac{1}{30} = \frac{4}{30} = \frac{2}{15}$$

$$\therefore k_e = 7.5$$

Then  
 $k_e = 7.5 + 20$

$$\boxed{k_e = 27.5 \text{ N/m}}$$

4.  $k_1 = 100$  &  $k_2 = 200$  &  $k_3 = 100$



$$k_e = 100 + 200 = 300 \text{ N/m}$$

Then

$$\frac{1}{k_e} = \frac{1}{300} + \frac{1}{100}$$

$$\frac{1}{k_e} = \frac{4}{300} = \frac{1}{75}$$

$$\boxed{k_e = 75 \text{ N/m}}$$

5. Imagine you have three identical springs, each with a spring constant of 10 N/m. Using all three springs, what is the largest effective spring constant you could make?

All in parallel, so  $k_e = 10 + 10 + 10 = \boxed{30 \text{ N/m}}$

6. Imagine you have three identical springs, each with a spring constant of 10 N/m. Using all three springs, how could you make an effective spring constant of 15 N/m?



The top 2 are in series:  
 $\frac{1}{k_e} = \frac{1}{10} + \frac{1}{10}$

$$k_e = 5$$

Then that is in parallel with the third

$$\text{so } k_e = 5 + 10 = \boxed{15 \text{ N/m}}$$

7. Imagine you have three identical springs, each with a spring constant of 10 N/m. Could you make an effective spring constant that was less than 10 N/m? (If yes, show how and give result.)

Connect in series! So  $\frac{1}{k_e} = \frac{1}{10} + \frac{1}{10} + \frac{1}{10} = \frac{3}{10}$

$$\text{So } \boxed{k_e = \frac{10}{3} \text{ N/m}}$$

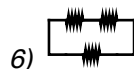
Answers: 1) 30 N/m

2) 125 N/m

3) 27.5 N/m

4) 75 N/m

5) 30 N/m, all in parallel



6)

7) 3.33 N/m, all in series